7-3 Study Guide and Intervention

Rational Exponents

Rational Exponents For any real numbers a and b and any positive integer n, if $a^n = b$, then a is an nth root of b. Rational exponents can be used to represent nth roots.

Square Root	$b^{\frac{1}{2}} = \sqrt{b}$
Cube Root	$b^{\frac{1}{3}} = \sqrt[3]{b}$
nth Root	$b^{\frac{1}{n}} = \sqrt[n]{b}$

Example 1 Write $(6xy)^{\frac{1}{2}}$ in radical

form.

$$(6xy)^{\frac{1}{2}} = \sqrt{6xy}$$

Definition of $b^{\frac{1}{2}}$

Example 2 Simplify $625^{\frac{1}{4}}$.

$$625^{\frac{1}{4}} = \sqrt[4]{625} \qquad b^{\frac{1}{n}} = \sqrt[n]{b}$$

$$= \sqrt[4]{5 \cdot 5 \cdot 5 \cdot 5} \qquad 625 = 5^{4}$$

$$= 5 \qquad \text{Simplify.}$$

Exercises

Write each expression in radical form, or write each radical in exponential form.

1.
$$14^{\frac{1}{2}}\sqrt{14}$$

2.
$$5x^{\frac{1}{2}}$$
 5 \sqrt{x}

3.
$$17y^{\frac{1}{2}}$$
 17 \sqrt{y}

4.
$$12^{\frac{1}{2}}\sqrt{12}$$

5.
$$19ab^{\frac{1}{2}}$$
 19 $a\sqrt{b}$

6.
$$\sqrt{17}$$
 17 $\frac{1}{2}$

7.
$$\sqrt{12n}$$
 (12n) $^{\frac{1}{2}}$

8.
$$\sqrt{18b}$$
 (18b) $^{\frac{1}{2}}$

9.
$$\sqrt{37}$$
 37 $\frac{1}{2}$

Simplify.

10.
$$\sqrt[3]{343}$$
 7

11.
$$\sqrt[5]{1024}$$
 4

12.
$$512^{\frac{1}{3}}$$
 8

13.
$$\sqrt[4]{2401}$$
 7

14.
$$\sqrt[6]{64}$$
 2

15.
$$243^{\frac{1}{5}}$$
 3

16.
$$\sqrt[3]{1331}$$
 11

17.
$$\sqrt[4]{6561}$$
 9

18.
$$4096^{\frac{1}{4}}$$
 8

Lesson 7-3

Study Guide and Intervention (continued) 7-3

Rational Exponents

Solve Exponential Equations In an exponential equation, variables occur as exponents. Use the Power Property of Equality and the other properties of exponents to solve exponential equations.

Example

Solve $1024^{x-1} = 4$.

$$1024^{x-1} = 4$$

Original equation

$$(4^5)^{x-1} = 4$$

Rewrite 1024 as 45.

$$4^{5x-5}=4^1$$

Power of a Power, Distributive Property

$$5x - 5 = 1$$

Power Property of Equality

$$5x = 6$$

Add 5 to each side.

$$x = \frac{6}{5}$$

Divide each side by 5.

Exercises

Solve each equation.

1.
$$2^x = 128$$
 7

2.
$$3^{3x+1} = 81$$
 1

3.
$$4^{x-3} = 32\frac{11}{2}$$

4.
$$5^x = 15,625$$
 6

5.
$$6^{3x+2} = 216 \frac{1}{3}$$

6.
$$4^{5x-3} = 16$$
 1

7.
$$8^x = 4096$$
 4

$$8.9^{3x+3} = 6561 \frac{1}{3}$$

9.
$$11^{x-1} = 1331$$
 4

10.
$$3^x = 6561$$
 8

11.
$$2^{5x+4} = 512$$
 1

12.
$$7^{x-2} = 343$$
 5

13.
$$8^x = 262,144$$
 6

14.
$$5^{5x} = 3125$$
 1

15.
$$9^{2x-6} = 6561$$
 5

16.
$$7^x = 2401$$
 4

17.
$$7^{3x} = 117,649$$
 2

18.
$$6^{2x-7} = 7776$$
 6

19.
$$9^x = 729$$
 3

20.
$$8^{3x+1} = 4096$$
 1

21.
$$13^{3x-8} = 28,561$$
 4